

NO Reading assignment

H.W Due today

Bonus H.W available
(can go over 100% in H.W)

OZL updated

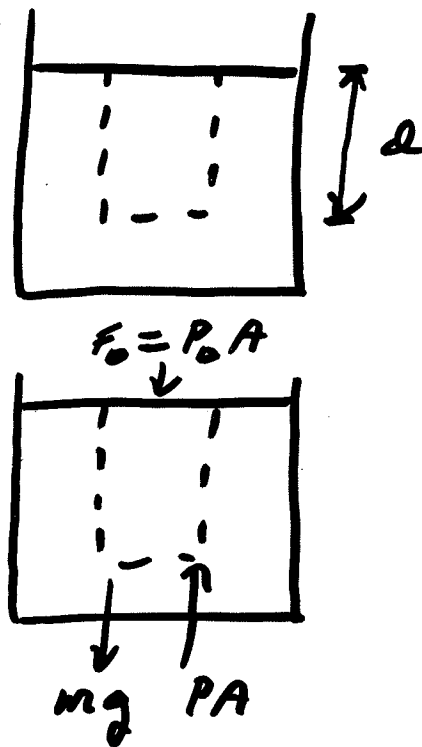
Properties of pressure in a fluid

- 1) At any point that a fluid is in contact with a surface, the pressure is exerted perpendicular to surface
- 2) At any point inside a fluid, pressure is directed in all directions with same magnitude
- 3) Pressure at any point depends only on the depth of the point

Suppose there is a volume of fluid with a uniform density which has a depth d and area A

What forces act on this volume of fluid?

$$\Sigma F_y = 0$$



$$PA - mg - P_0 A = 0$$

$$PA - \rho V g - P_0 A = 0$$

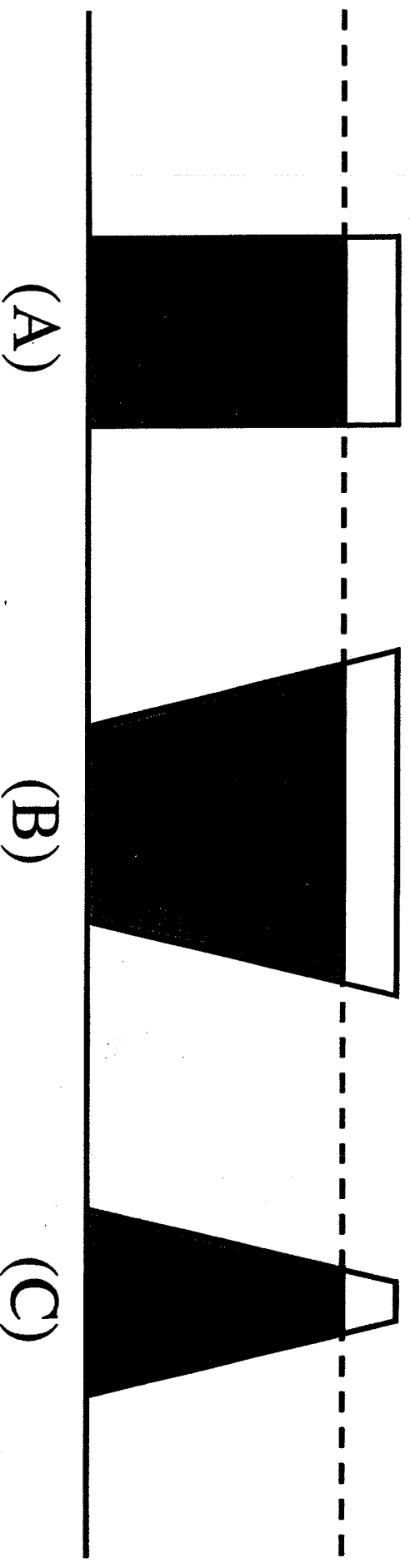
$$PA - \rho d A g - P_0 A = 0$$

$$P - \rho d g - P_0 = 0$$

$$P = P_0 + \rho g d$$

Interactive Question

Three drinking glasses all have the same area base and are all filled to the same level. Which glass has the greatest liquid pressure at the bottom?



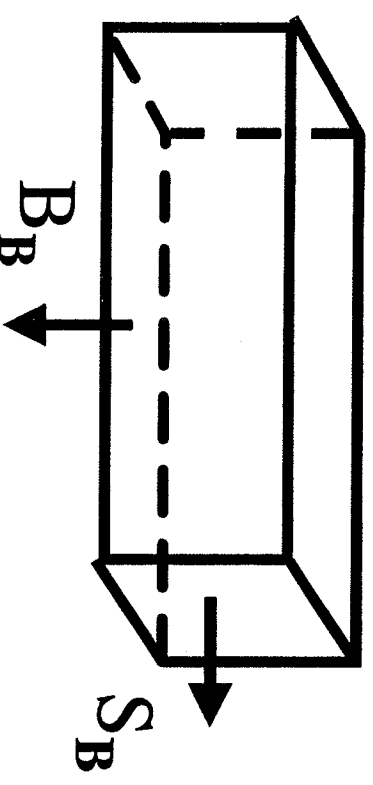
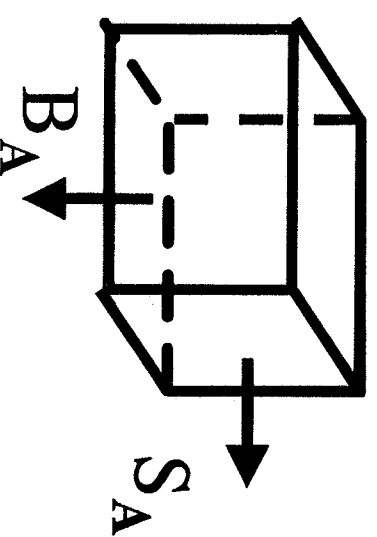
- A) Glass A
- B) Glass B
- C) Glass C
- D) All have the same pressure

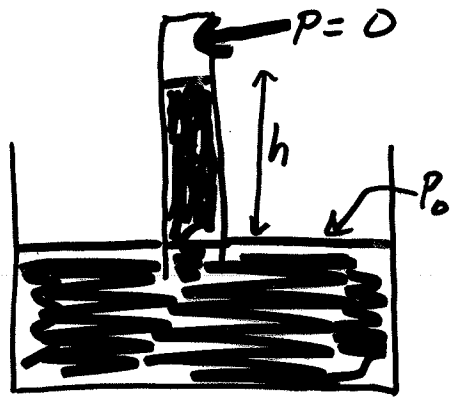
Interactive Question

Consider two fish tanks that are the same height and the same width. Tank **A** is 3 feet long and tank **B** is 6 feet long. S_A is the force on the side of tank **A**, and S_B is force on the side of tank **B**. B_A is the force on the bottom of tank **A**, and B_B is force on the bottom of tank **B**.

Which statement below is true?

- A) $S_A = S_B$ and $B_A = B_B$
- B) $S_A = 2S_B$ and $B_A = B_B$
- C) $2S_A = S_B$ and $2B_A = B_B$
- D) $S_A = S_B$ and $2B_A = B_B$
- E) $S_A = 2S_B$ and $B_A = 2B_B$



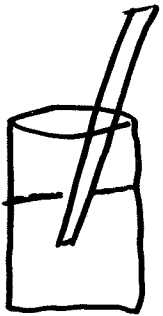


measurements of
pressure

$$P_0 = \rho g h$$

for mercury at atmospheric pressure $P_0 \approx 760 \text{ mm}$
water $P_0 \approx 10.3 \text{ m}$

Can I suck water through a straw 15 m long?



NO

Pascal's principle

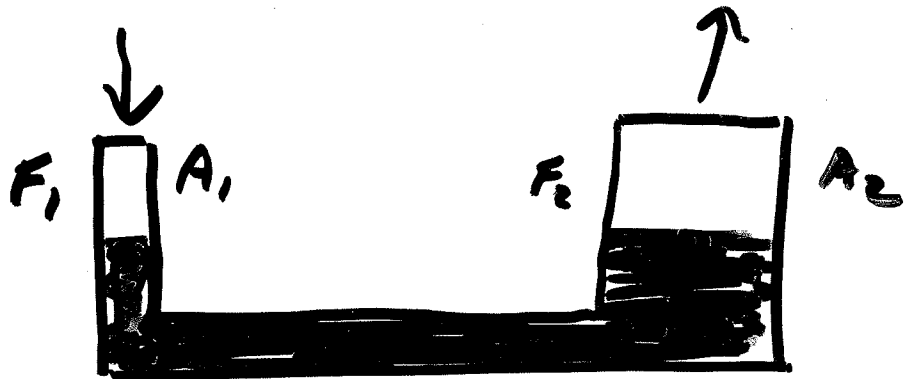
$$P = P_0 + \rho gh$$

IF external pressure increases, total pressure increases by same amount

Pressure applied to a confined fluid increases the pressure throughout by the same amount

hydraulic lift

$$P_1 = \frac{F_1}{A_1} \quad P_2 = \frac{F_2}{A_2}$$



Pascal's principle $\Rightarrow P_1 = P_2$

$$\frac{F_1}{A_1} = \frac{F_2}{A_2} \Rightarrow \boxed{F_2 = F_1 \left(\frac{A_2}{A_1} \right)}$$

if $A_2 > A_1$ $F_2 > F_1$

ex) A hydraulic press is used in a trash compactor

radius of input piston = $6.4 \times 10^{-3} \text{ m}$

radius of output piston = $5.1 \times 10^{-2} \text{ m}$

if input force is 330 N , what is output force?

$$F_2 = F_1 \left(\frac{A_2}{A_1} \right)$$

$$F_2 = (330 \text{ N}) \left(\frac{\pi (5.1 \times 10^{-2} \text{ m})^2}{\pi (6.4 \times 10^{-3} \text{ m})^2} \right)$$

$$\boxed{21,000 \text{ N}}$$

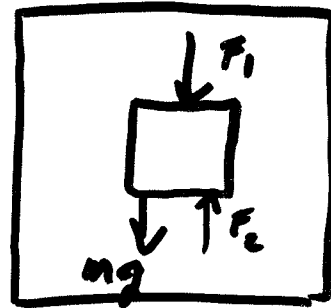
Buoyancy

Any object partially or totally submerged in a liquid has a buoyant force

⇒ Archimedes' principle

Any body completely or partially submerged in a fluid is buoyed up by a force equal to the weight of the fluid displaced by the body

object submerged in a liquid



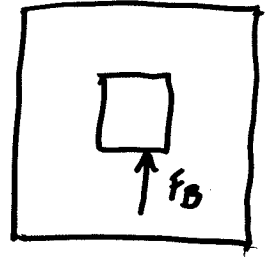
$$\begin{aligned}\Sigma F_y &= F_2 - F_1 - mg \\ &= P_2 A - P_1 A - mg \\ &= \rho g h_2 A - \rho g h_1 A - mg \\ &= \rho g A (h_2 - h_1) - mg \\ &= \rho g V - mg \\ &= \underset{\substack{\uparrow \\ F_B}}{m_f g} - mg\end{aligned}$$

$$F_B = W_{\text{fluid}} = m_{\text{fluid}} g = \rho_f V_f g$$

Buoyancy

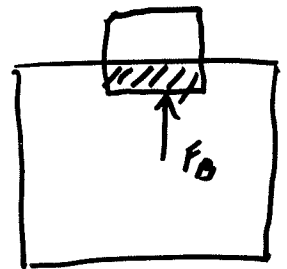
object which is submerged in a fluid

$$F_B = \rho_f V_{\text{object}} g$$



object is floating in a liquid

$$F_B = \rho_f V_f g$$



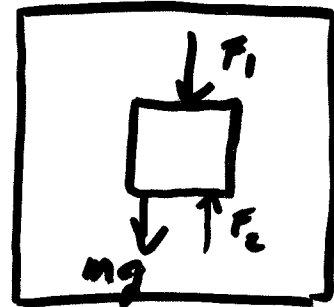
Buoyancy

Any object partially or totally submerged in a liquid has a buoyant force

⇒ Archimedes' principle

Any body completely or partially submerged in a fluid is buoyed up by a force equal to the weight of the fluid displaced by the body

object submerged in a liquid



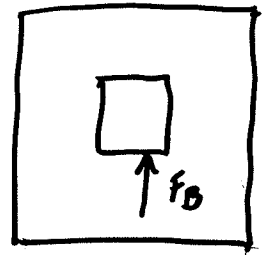
$$\begin{aligned}\Sigma F_y &= F_2 - F_1 - mg \\ &= P_2 A - P_1 A - mg \\ &= \rho g h_2 A - \rho g h_1 A - mg \\ &= \rho g A (h_2 - h_1) - mg \\ &= \rho g V - mg \\ &= \underset{\substack{\uparrow \\ F_B}}{m_{\text{fluid}} g} - mg\end{aligned}$$

$$F_B = W_{\text{fluid}} = m_{\text{fluid}} g = \rho_{\text{fluid}} V_{\text{fluid}} g$$

Buoyancy

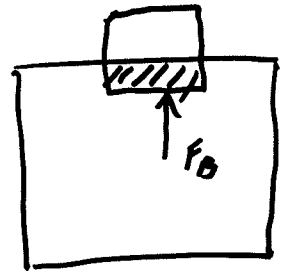
object which is submerged in a fluid

$$F_B = \rho_f V_{\text{object}} g$$



object is floating in a liquid

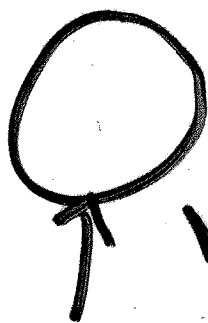
$$F_B = \rho_f V_f g$$



EX) What is buoyant force on a balloon filled with 1.0 m^3 Helium at sea level?

b) What is gravitational force on the balloon?

$$\begin{aligned} \text{a) } F_B &= \rho_f V g = \rho_A V_{\text{balloon}} g \\ &= (1.29 \text{ kg/m}^3 \times 1 \text{ m}^3) (9.8 \text{ m/s}^2) \\ &= \boxed{12.6 \text{ N}} \end{aligned}$$



$$\begin{aligned} \text{b) } F_g &= mg = \rho_{\text{He}} V_{\text{He}} g \\ &= (0.179 \text{ kg/m}^3 \times 1 \text{ m}^3) (9.8 \text{ m/s}^2) \\ &= \boxed{1.75 \text{ N}} \end{aligned}$$