

today! Wednesday

Ch 9

Wednesday: start fluids

Read 10.1-10.5

Final Exam prep on class web page

makeup Exam Tuesday: see me if any  
(if missed Exam) Questions

Evaluations available

# Equilibrium

object at rest is an example

Forces are balanced so no

acceleration and no angular acceleration

→ Constant velocity ( $\dot{v}=0$ )

→ Constant angular velocity ( $\dot{\omega}=0$ )

If an object is not moving ( $\dot{v}=0$ ) / rotating ( $\dot{\omega}=0$ ) it is in equilibrium.

$$\rightarrow \Sigma \vec{F} = m\vec{a} \quad \Sigma \vec{\tau} = I\vec{\alpha}$$

$$\vec{a} = 0 \quad \vec{\alpha} = 0$$

$$\Sigma \vec{F} = 0 \quad (\text{Done this before})$$

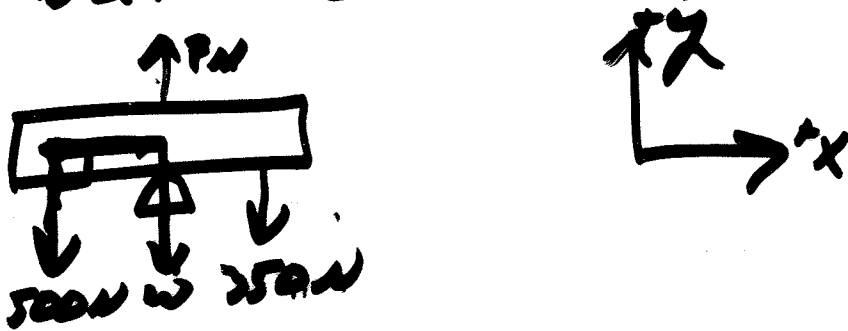
$$\Sigma \vec{\tau} = 0 \quad (\text{new})$$

$$\Sigma \tau = \Sigma r F \sin \theta = 0$$

Note Torque can be measured relative to any axis

ex) A uniform 40 N board supports 2 children weighing 500 N and 350 N. A support is under center of mass of board. The 500 N child is 1.5 m from center.

- a) what is Force that support exerts  
b) where should 350 N child sit to balance board?



$$F_N = ? \quad \Sigma F_y = 0$$

$$F_N - 500\text{ N} - 350\text{ N} - 40\text{ N} = 0$$

a)  $F_N = 890\text{ N}$

$$\sum \tau = 0$$

Choose support as axis of rotation



$$\tau_{F_s} = 0$$

$$\tau_w = 0$$

$$r = 0$$

$$\tau = r F \sin \theta$$

$$+ 500 \text{ N} \cdot 1.5 \text{ m} \sin 90^\circ - 350 \text{ N} \cdot r \cdot \sin 90^\circ = 0$$

$$r = 2.14 \text{ m from support}$$

Choose 500 N child as axis of rotation

$$\tau_{500} = 0$$

$$- 40 \text{ N} \cdot 1.5 \text{ m} \cdot \sin 90^\circ$$

$$+ 890 \text{ N} \cdot 1.5 \text{ m} \cdot \sin 90^\circ$$

$$- 350 \text{ N} \cdot r \cdot \sin 90^\circ = 0$$

$$r = 3.64 \text{ m from 500 N child}$$

$$3.64 - 1.5 \text{ m} = 2.14 \text{ m from support}$$

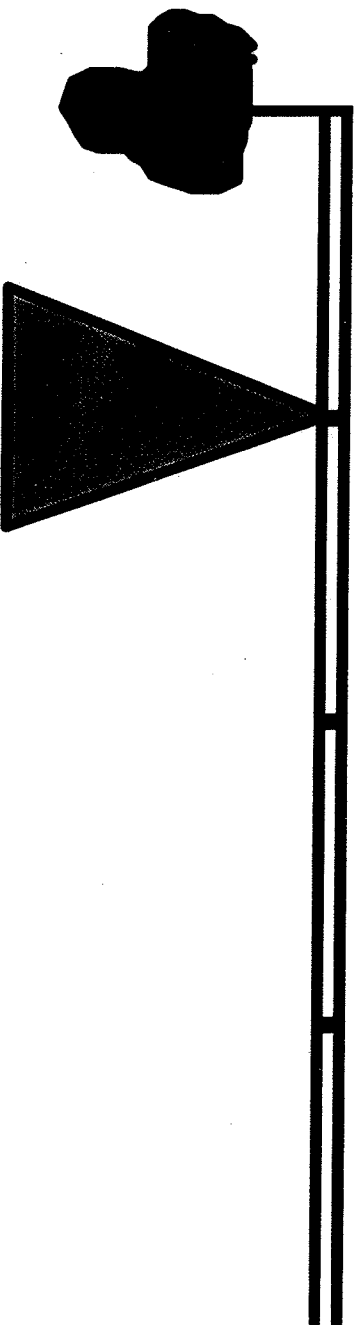
## Interactive Question

A heavy boy and a lightweight girl are balanced on a massless seesaw. If they both move forward so that they are one-half their original distance from the pivot point, what will happen to the seesaw?

- A) The side the boy is sitting on will tilt downward.
- B) The side the girl is sitting on will tilt downward.
- C) Nothing, the seesaw will still be balanced.
- D) It is impossible to say without knowing the masses and the distances.

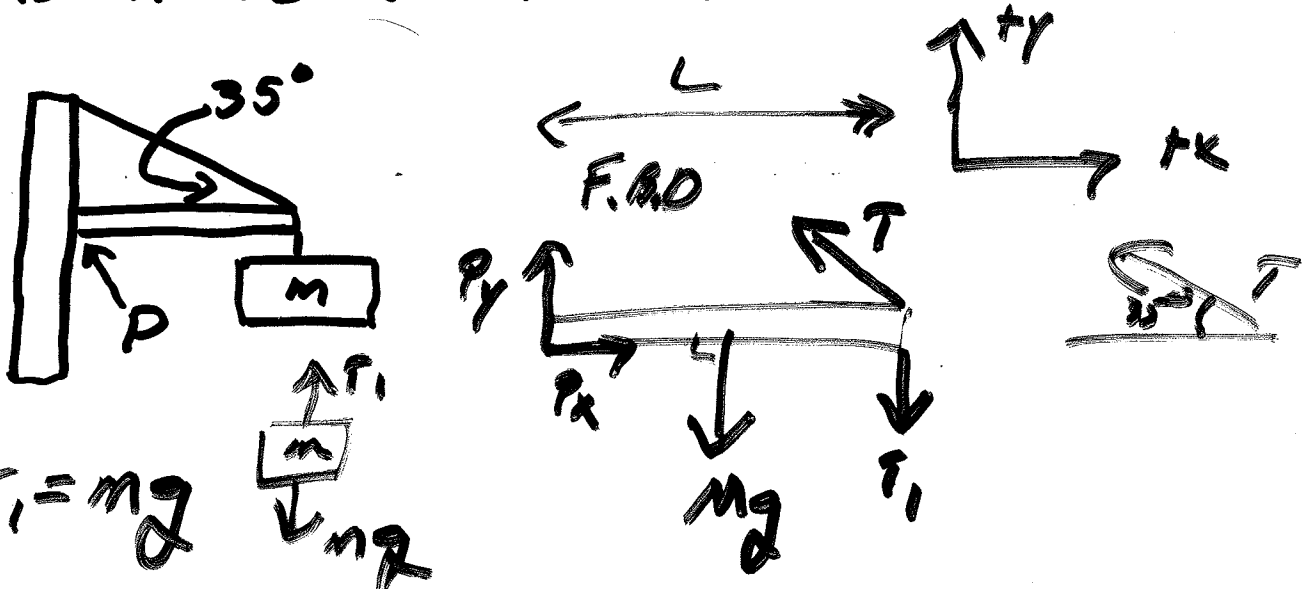
## Interactive Question

A 1-kg rock is suspended by a massless string from one end of a 1-m measuring stick. What is the weight of the measuring stick if it is balanced by a support force at the 0.25-m mark?



- A) 0.25 kg
- B) 0.5 kg
- C) 1kg
- D) 2 kg
- E) 3kg

ex) A 25 kg sign hangs from a 10 kg pole  
 what is Tension in wire and vertical  
 and horizontal forces on Pivot point P.



$$T_1 = mg$$

$$\sum F_x = 0 \quad P_x - T \cos 35^\circ = 0 \quad (1)$$

$$\sum F_y = 0 \quad P_y + T \sin 35^\circ - T_1 - Mg = 0 \quad (2)$$

$$\sum \tau = 0 \quad -Mg \left( \frac{L}{2} \right) \sin 90^\circ - T_1 L \sin 90^\circ + T L \sin 35^\circ = 0 \quad (3)$$

algebra (3)  $-Mg \left( \frac{L}{2} \right) - T_1 L + T \sin 35^\circ = 0$

$$T = \frac{Mg \frac{L}{2} + T_1 L}{\sin 35^\circ} = \boxed{510 \text{ N}} \quad T_1 = mg$$

$$(1) \quad P_x = T \cos 35^\circ = \boxed{420 \text{ N}}$$

$$(2) \quad P_y = Mg + mg - T \sin 35^\circ = \boxed{50 \text{ N}}$$