

NO Reading assignment  
H.W Due Friday

Action Center Thursday

Group problem

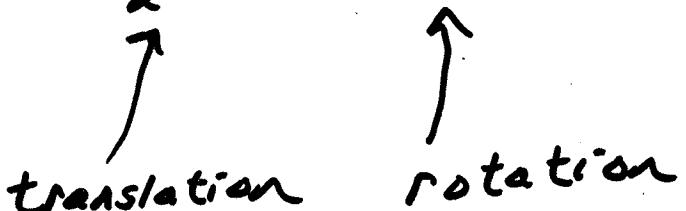
Torque and Moments of  
Inertia

D2L updated

# Review

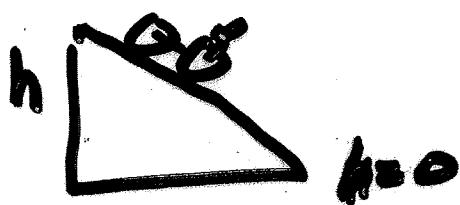
$$K.E \text{ rolling } \frac{1}{2} I \omega^2$$

$$\text{Total K.E} = \frac{1}{2} m v^2 + \frac{1}{2} I \omega^2$$



translation      rotation

ex) Two bicycles roll down a hill 20 m high. Both have a mass of 12 kg and wheels of radius .35 m. 1<sup>st</sup> bicycle has wheels that are 0.6 kg each. 2<sup>nd</sup> bicycle has wheels that are 0.3 kg each. Which bicycle has faster speed at bottom?



conservue Energy  
 $K_i + U_i = K_f + U_f$

$$0 + mgh = \left( \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2 \right) + 0$$

$$mgh = \frac{1}{2}mv^2 + 2 \cdot \frac{1}{2}I\omega^2$$

↑  
bike mass      ↑  
tires      ↑  
Tire mass

$$mgh = \frac{1}{2}mv^2 + (Mg^2)(\frac{v}{R})^2$$

$$\omega = \frac{v}{R}$$

$$mgh = \frac{1}{2}mv^2 + Mv^2$$

$$v = \sqrt{\frac{mgh}{\frac{1}{2}m + M}}$$

$$M = 0.3 \text{ kg} \quad v = 19.3 \text{ m/s}$$

$$M = 0.6 \text{ kg} \quad v = 18.9 \text{ m/s}$$

## Interactive Question

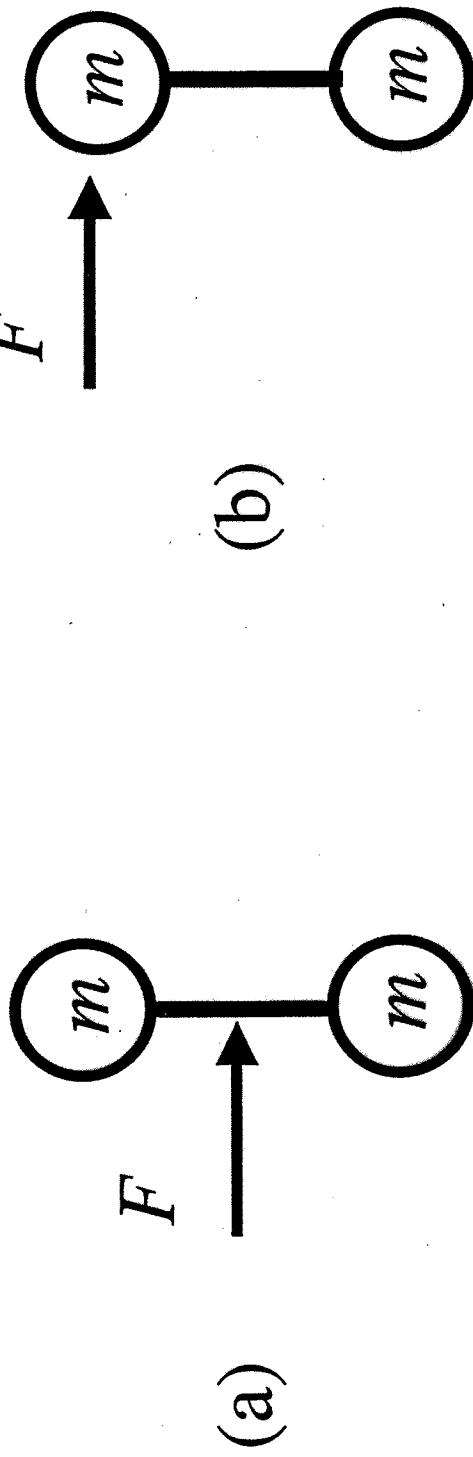
A solid sphere (S), a thin hoop (H), and a solid disk (D), all with the same radius, are allowed to roll down an inclined plane without slipping. In which order will they arrive at the bottom? (The first one down listed first).

$$\begin{aligned}I_S &= \frac{2}{5}mR^2 \\I_H &= mR^2 \\I_D &= \frac{1}{2}mR^2\end{aligned}$$

- A) H,D,S
- B) H,S,D
- C) S,D,H
- D) S,H,D
- E) D,H,S

## Interactive Question

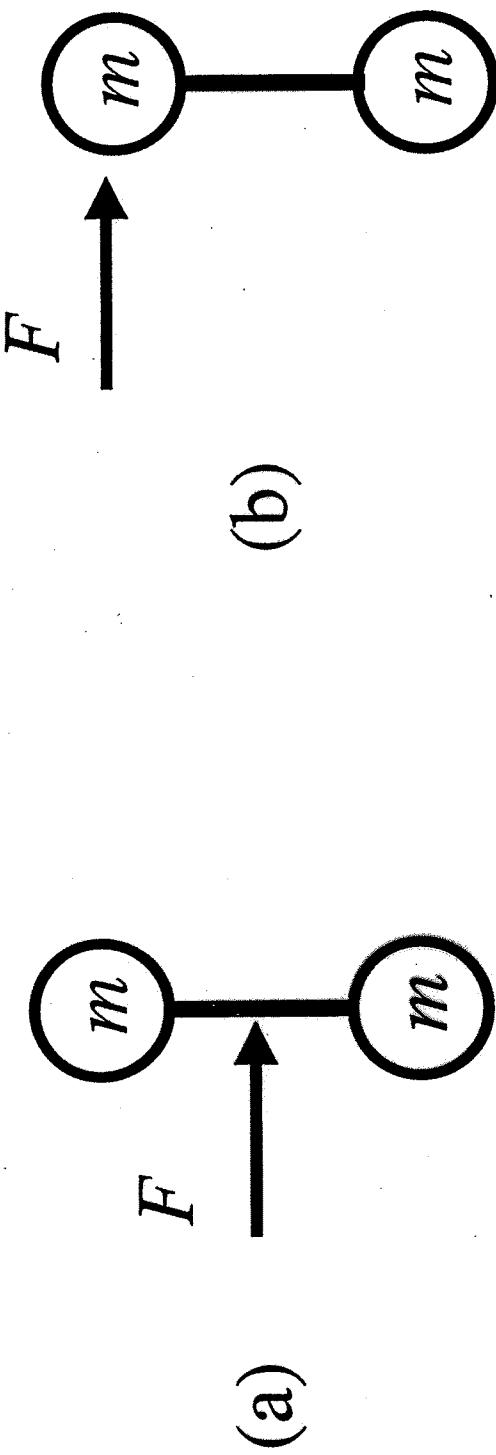
A force  $F$  is applied to a dumbbell for a time interval  $\Delta t$ , first as in (a) and then as in (b). In which case does the dumbbell acquire the greater energy?



- A) (a)
- B) (b)
- C) no difference

## Interactive Question

A force  $F$  is applied to a dumbbell for a time interval  $\Delta t$ , first as in (a) and then as in (b). In which case does the dumbbell acquire the greater center-of-mass speed?



- A) (a)
- B) (b)
- C) no difference

# Conservation of angular momentum

We know linear momentum ( $\vec{p}$ ) is conserved  
 Let's look at angular momentum

## Linear

Force ( $F$ )

Kinetic Energy  
 $\frac{1}{2}mv^2$

Linear momentum

$$\vec{p} = m\vec{v}$$

## Angular

Torque ( $\tau$ )

$$\frac{1}{2}I\omega^2$$

angular momentum

$$\vec{L} = I\vec{\omega}$$

$$\sum \vec{F} = m\vec{a} = \frac{d\vec{p}}{dt}$$

linear momentum  
 conserved if no  
 net external forces

$$\sum \vec{p}_i = \sum \vec{p}_f$$

$$\sum \vec{\tau} = I\vec{\alpha} = \frac{d\vec{L}}{dt}$$

angular momentum  
 conserved if no  
 net external torques

$$\sum \vec{L}_i = \sum \vec{L}_f$$

$$\sum I_i \omega_i = \sum I_f \omega_f$$

$$\sum m r_i^2 \omega_i = \sum m r_f^2 \omega_f$$